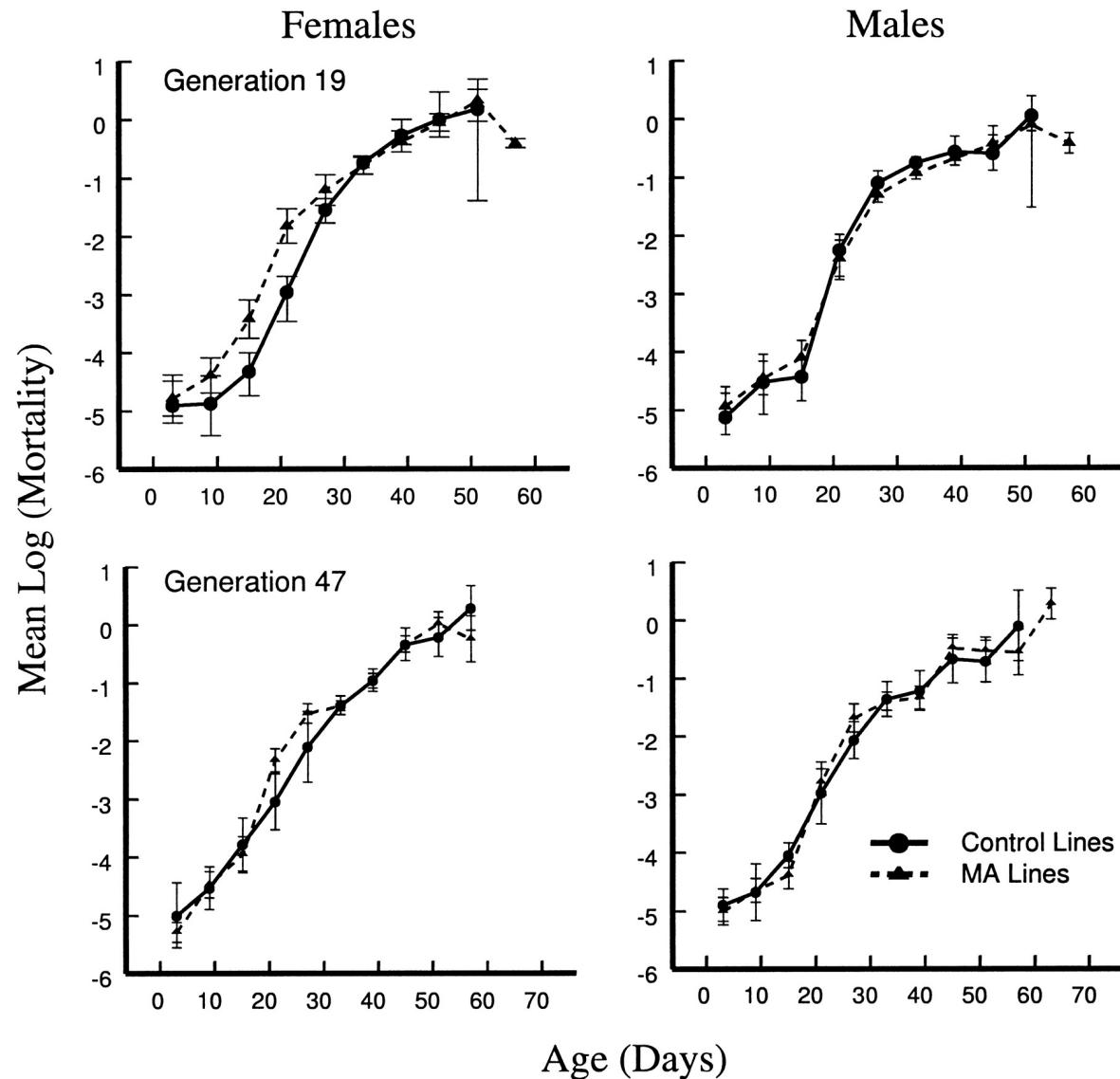
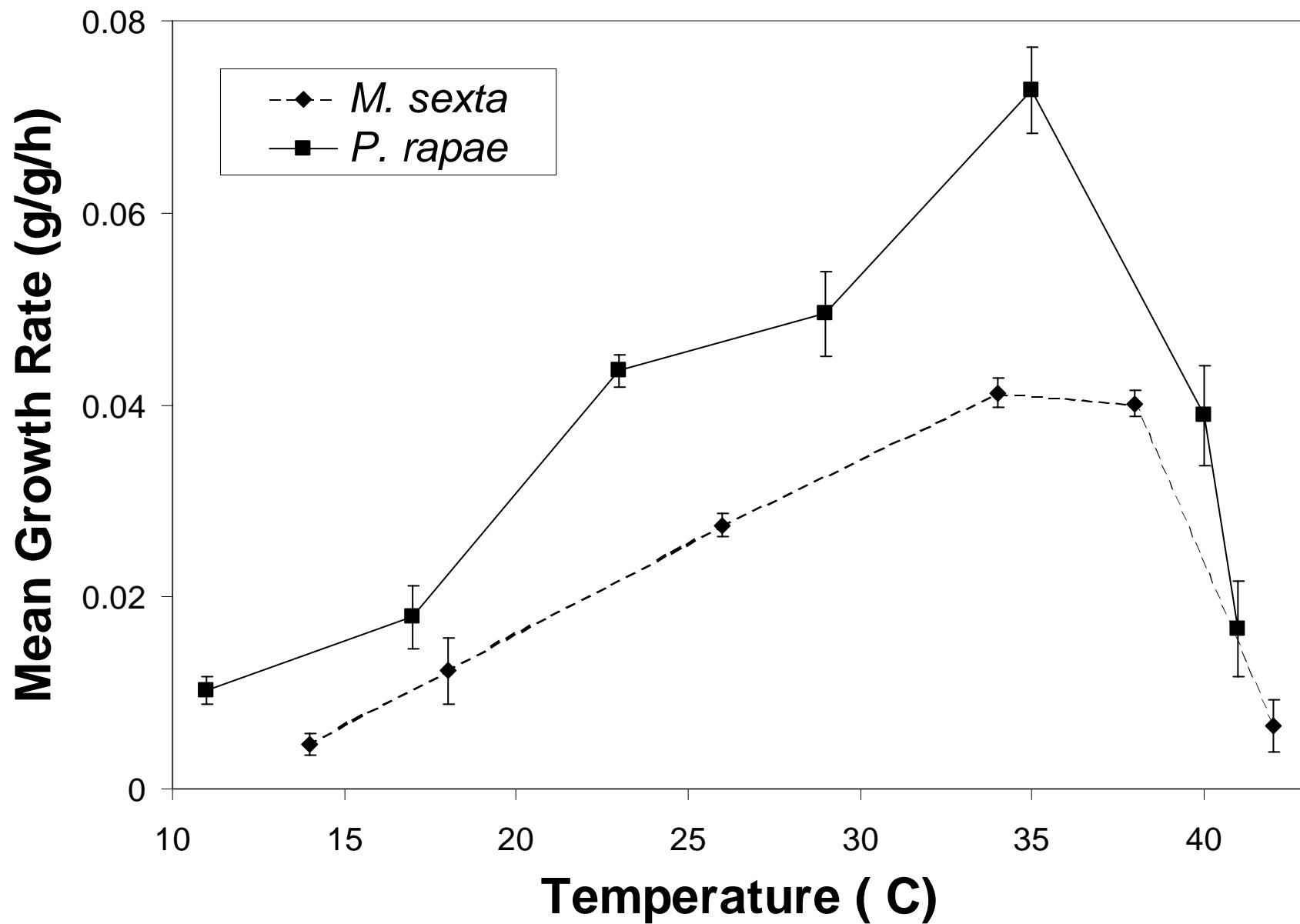


# Evolution of functional traits (Recap)

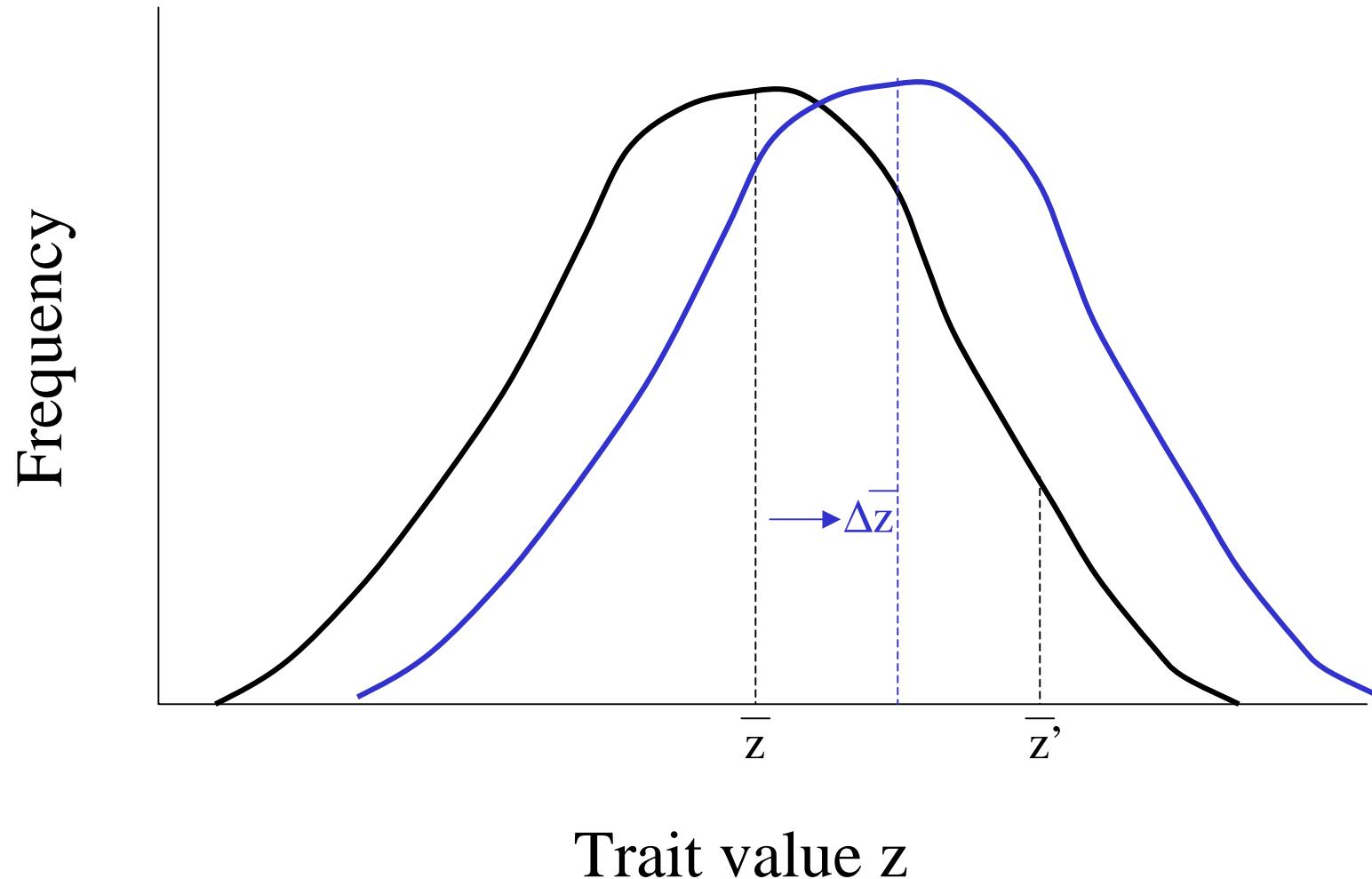
- Traits as functions: functional, function-valued, infinite-dimensional
- A primer in evolutionary models:
  - Variation, inheritance, selection, evolution
- Approaches to analysing functional traits:
  - understanding and estimating genetic variation

Age-specific mortality rates (*Drosophila*)  
Pletcher et al, Genetics (1999)





# Evolution, in 3 easy steps (3)



# Evolution of quantitative traits: some basics

- Individual organism:
  - Phenotype: observable trait with value  $z$
  - Genotype: genetic ‘type’ (usually inferred)
- Population:
  - Phenotypic variance,  $P = G + E$
  - Genetic variance,  $G$
- Evolution = change in mean trait value per generation,  $\Delta\bar{z}$

# A simple evolutionary model

- Variation and inheritance
  - Variance:  $P = G + E$
- Selection
  - Selection gradient:  $\beta = P^{-1}(\bar{z}' - \bar{z})$
  - Also:  $\beta = d[\ln(\bar{W})]/dz$ , where  $\bar{W}$  = mean population fitness
- Evolutionary response
$$\Delta\bar{z} = G \beta$$

$$\Delta \bar{z} = G \beta$$

$z$  may be:

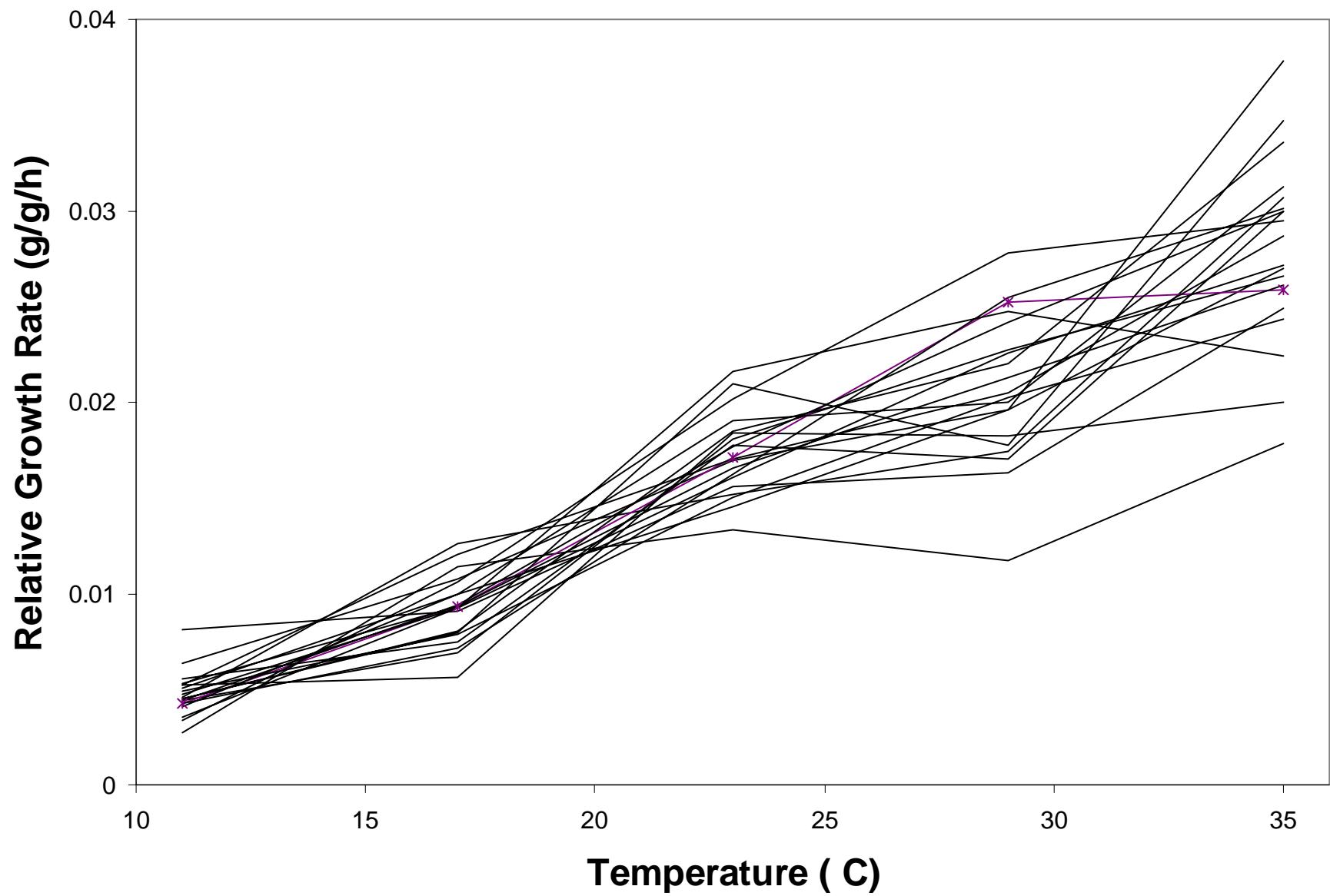
- a scalar
- a vector
- a function

$$\Delta \bar{z}(t) = \int G(t,s) \beta(s) ds$$

# Genetics recap: Temperature and caterpillar growth rate curves

- Genetic variation in TPCs
- Eigenfunction analysis

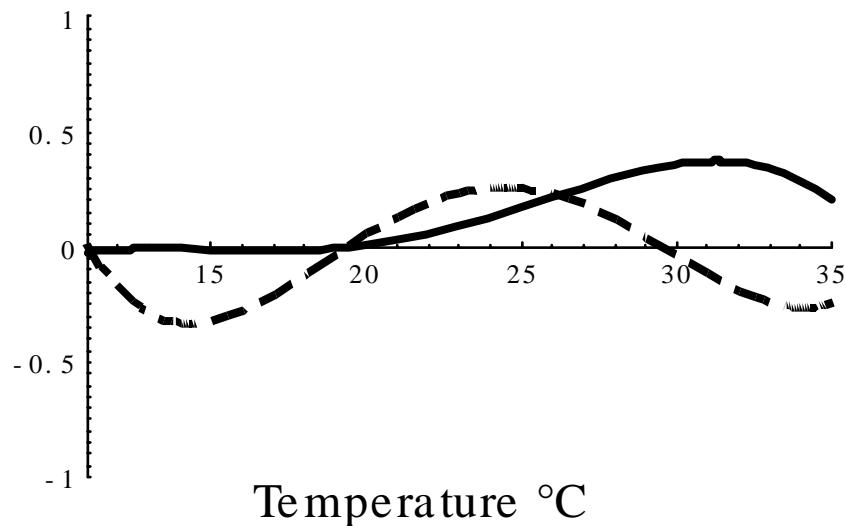




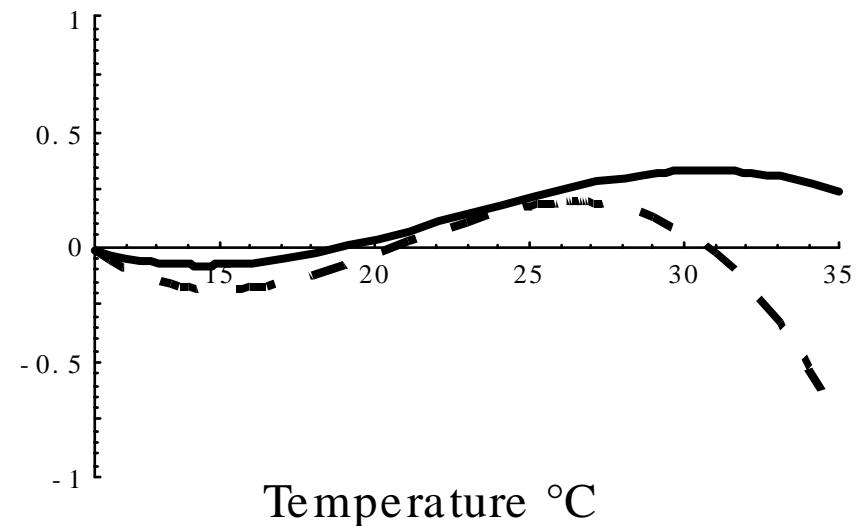
# Caterpillar growth rates

## Leading and Second Eigenfunctions

Full Fit



Smooth Fit



# Evolution of functional traits (Take II)

- Why does genetic variation ( $G$ ) matter?
  - Direct and indirect responses to selection
  - Constraints on directions of evolution
- Understanding selection
  - What is selection?
  - Selection on a functional trait: an example
  - Selection and environmental variation
- Predicting evolutionary trajectories

# Why G matters

G and the response to selection

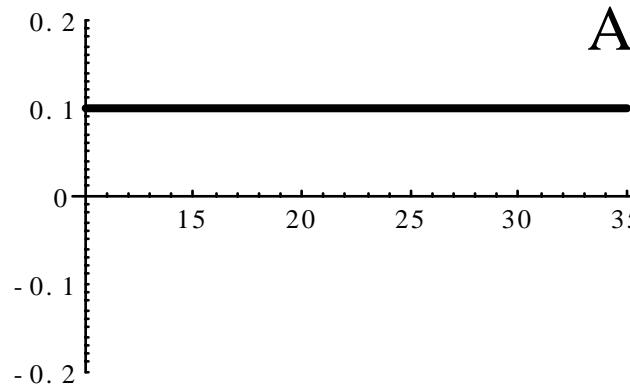
$$\Delta \bar{z}(t) = \int G(t, s) \beta(s) ds$$

Direct and indirect responses to selection

—

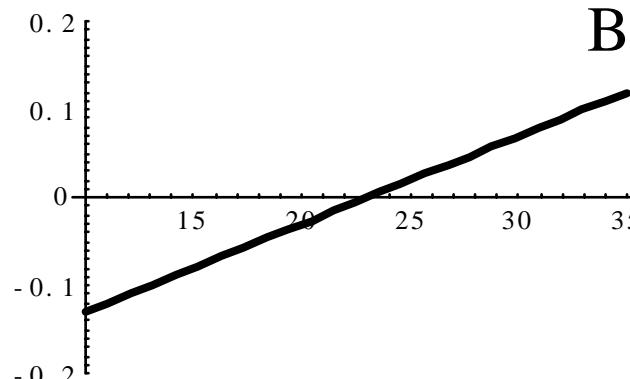
Constraints: when evolution won't go

# Eigenfunction



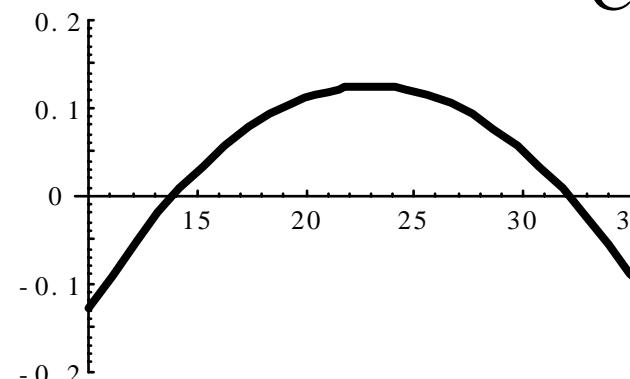
A

Faster-slower



B

Hotter-colder



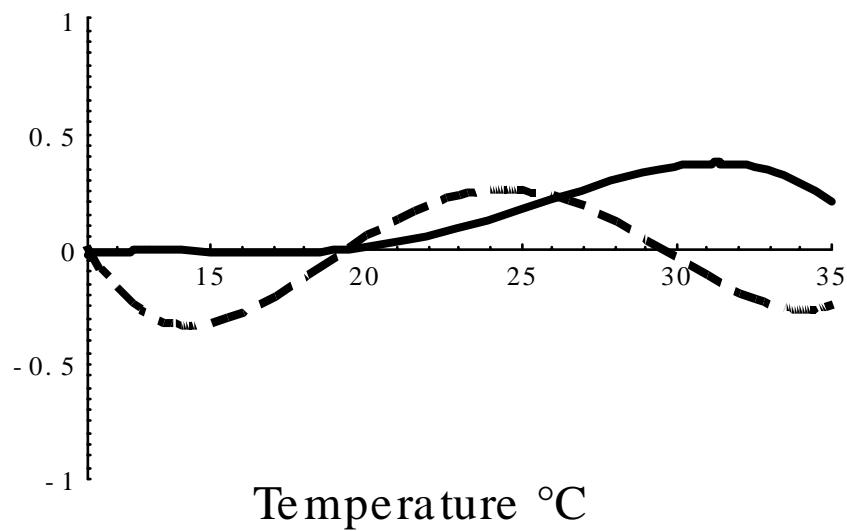
C

Generalist-specialist

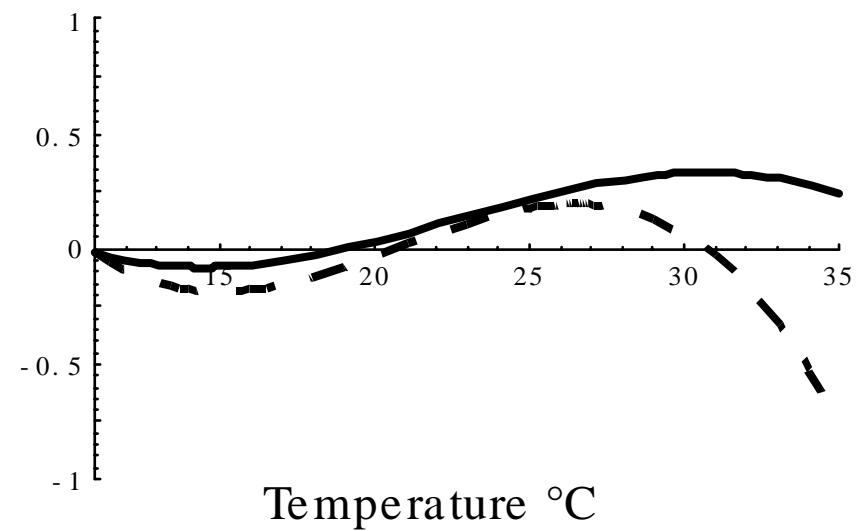
Temperature °C

# Leading and Second Eigenfunctions

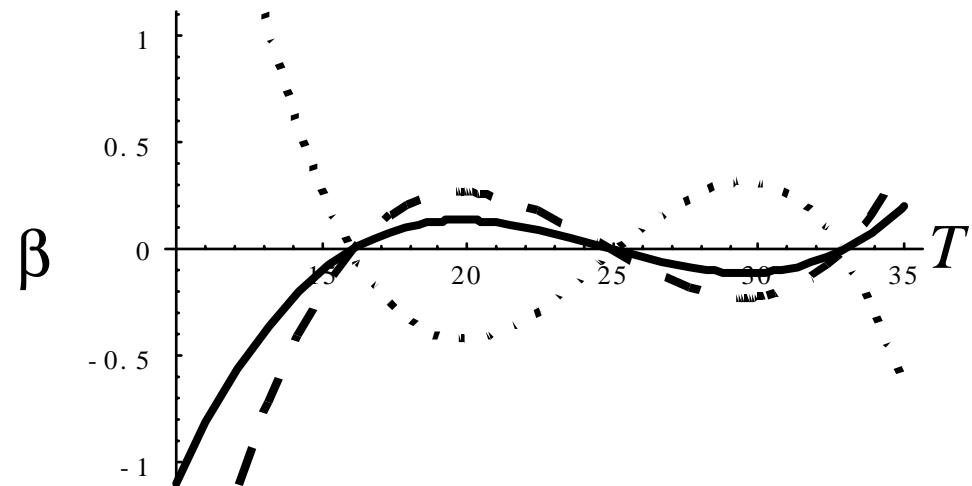
Full Fit



Smooth Fit



## Evolutionary Constraints: Identifying zero eigenfunctions

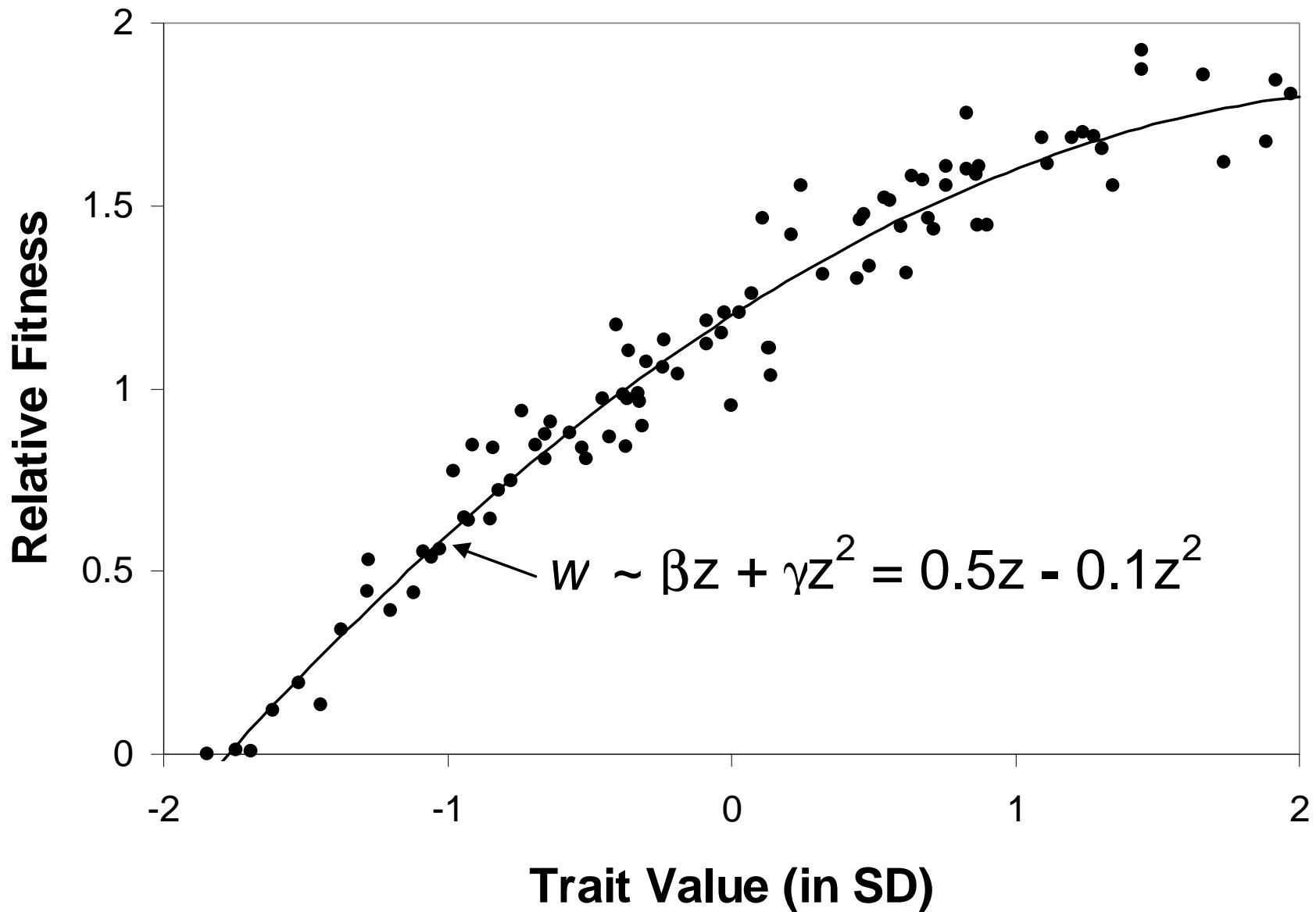


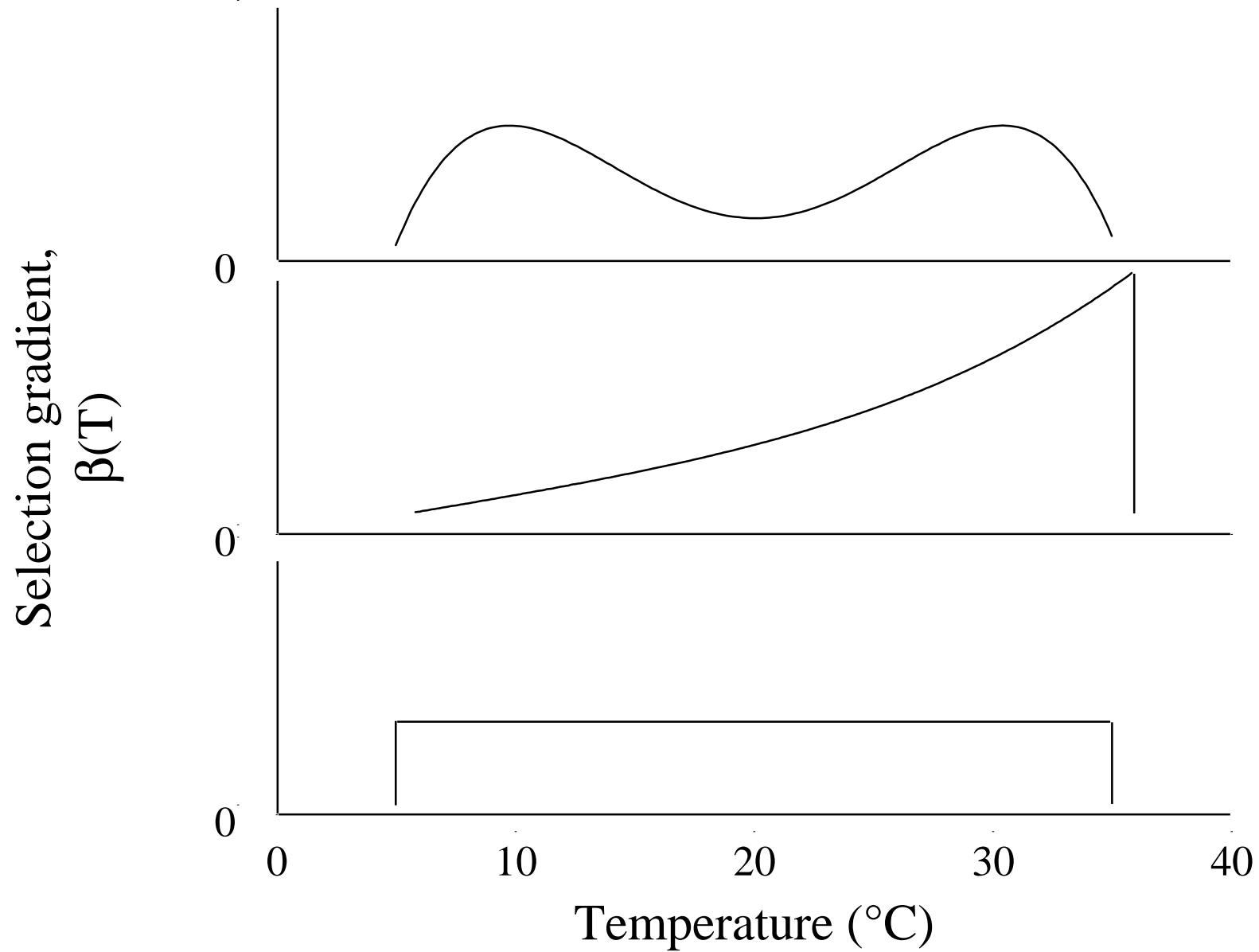
# Selection and evolutionary response

- What is selection?
- Estimating selection,  $\beta(s)$ : an example
- Predicting evolutionary responses

$$\Delta\bar{z}(t) = \int G(t, s) \beta(s) ds$$

# Estimating Selection



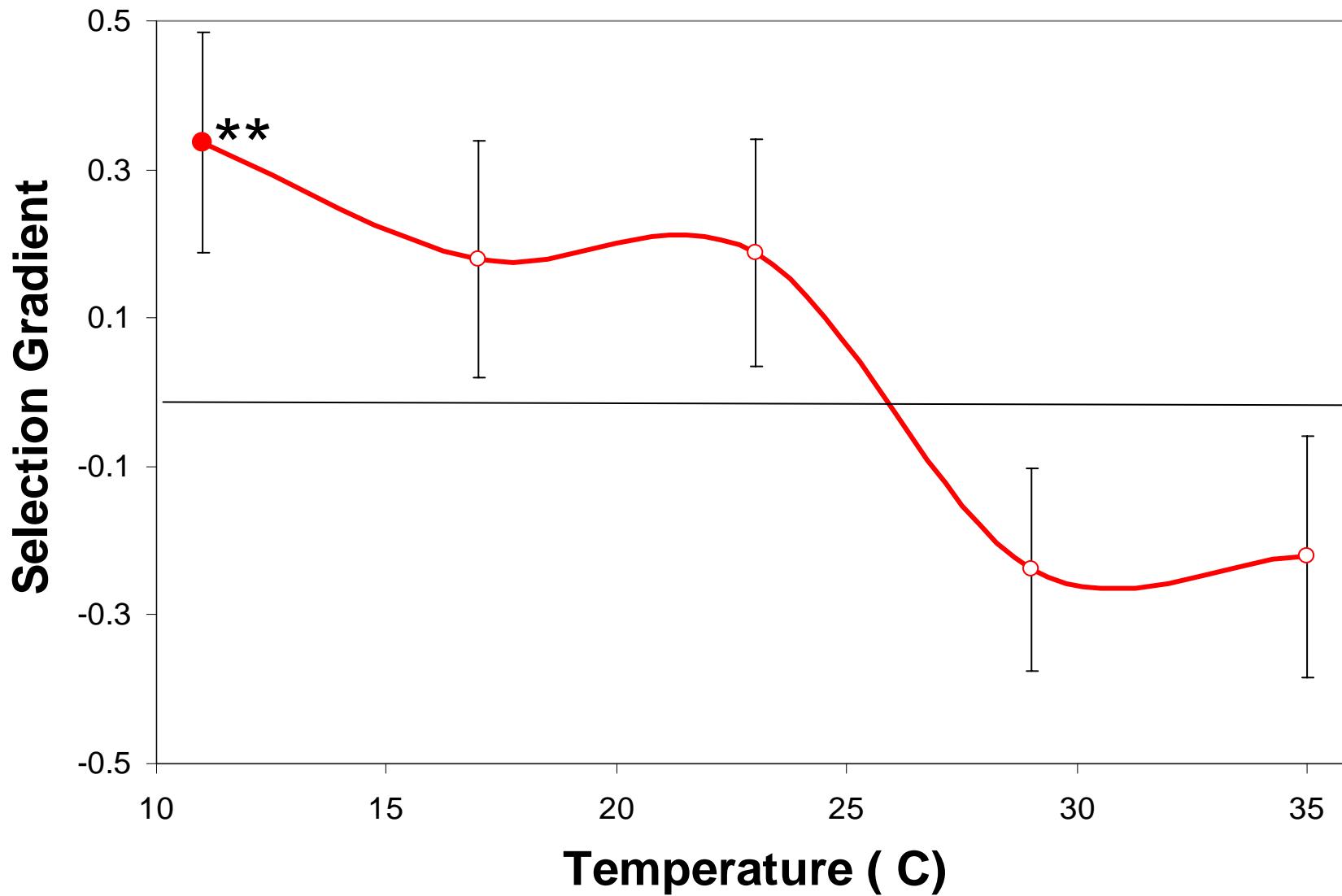


# Selection on caterpillar growth rate TPCs

- Measure  $z(T)$  for a sample of individuals in the lab --> estimate  $P(T, \theta)$
- Measure fitness of those individuals in the field (survival and time to pupation; pupal mass)
- Estimate  $\beta(T)$  (functional models?)

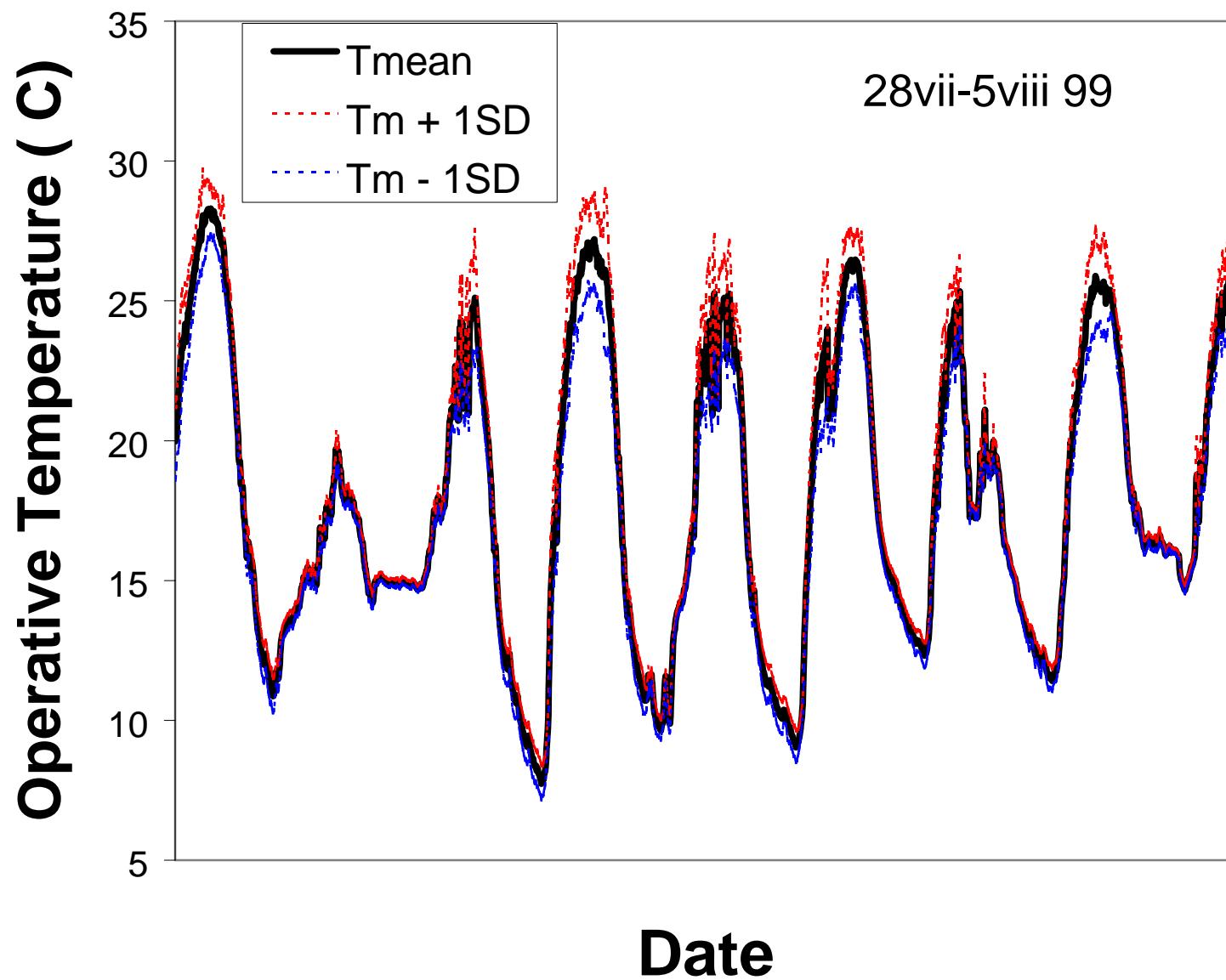


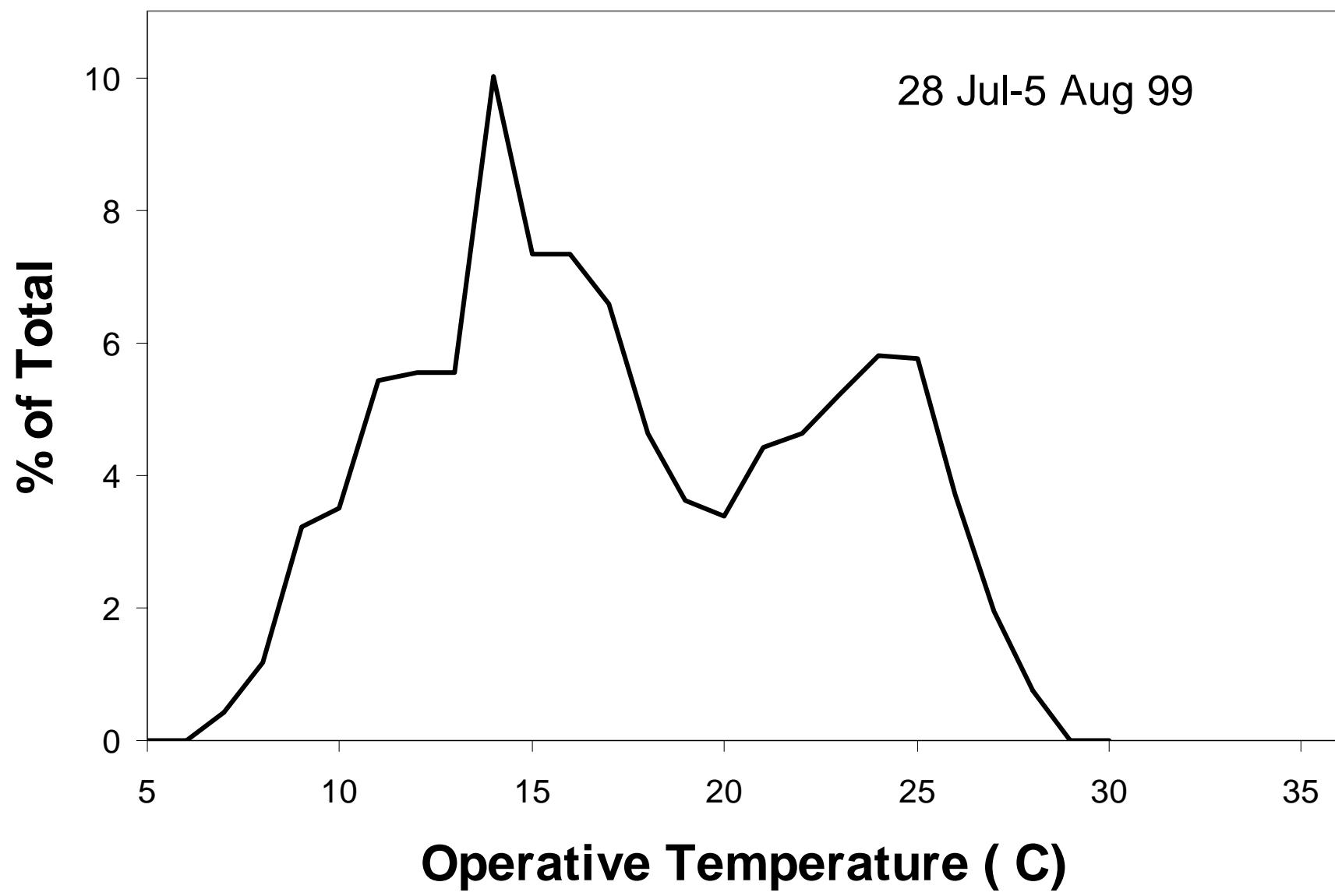
# Selection on Growth Rate

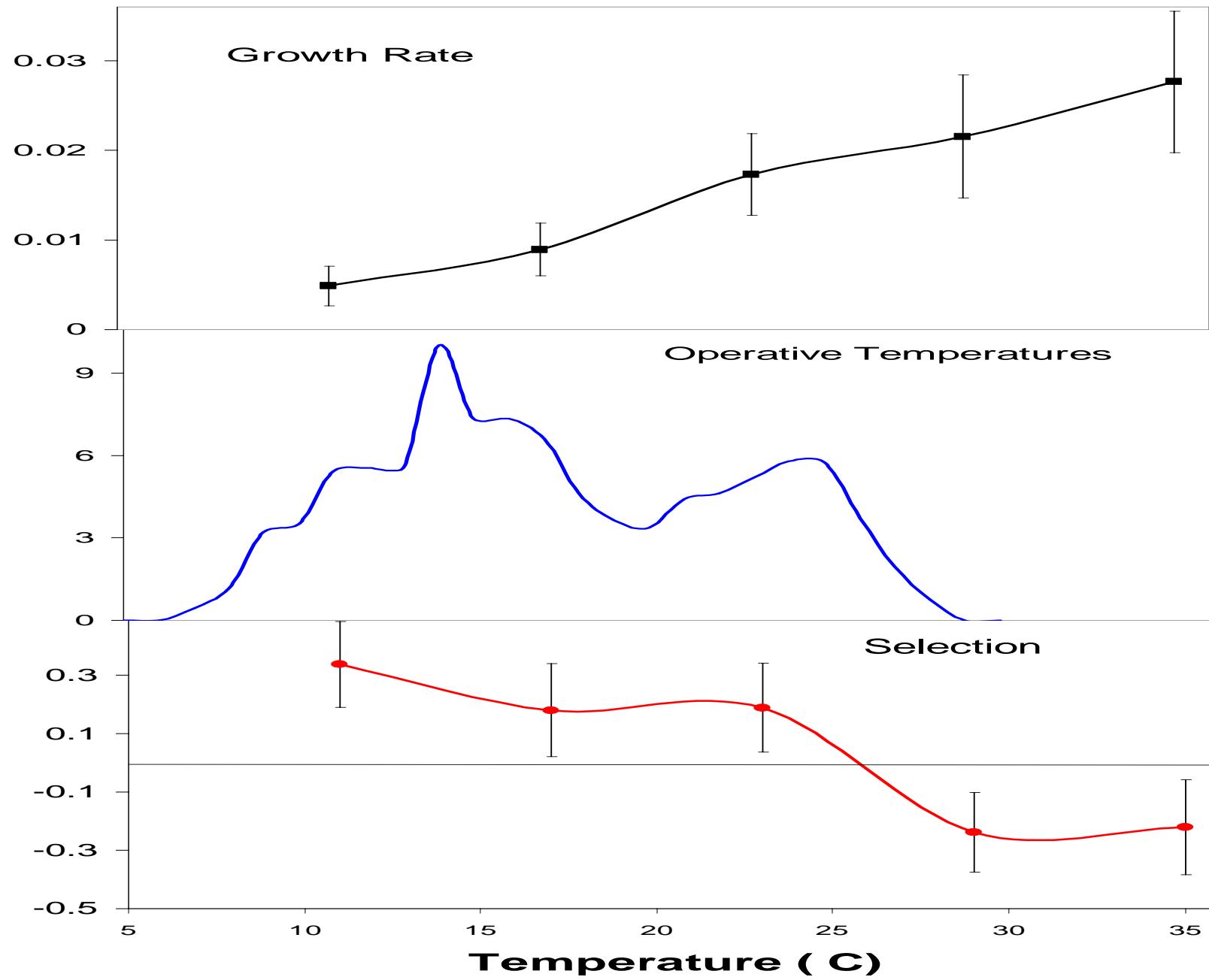


# Selection on TPC and environmental temperatures: Measuring ‘caterpillar’ temperatures







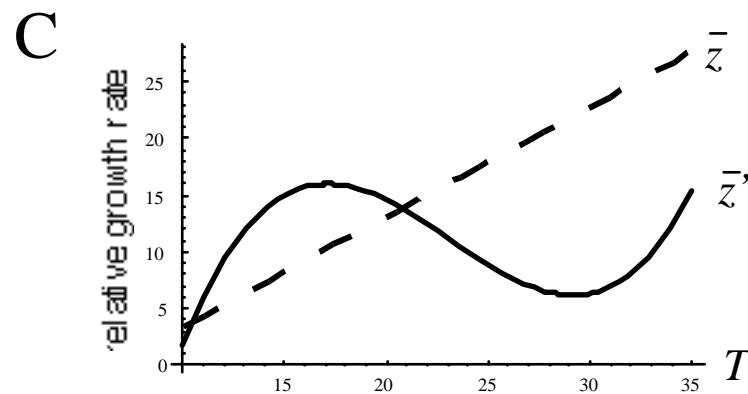
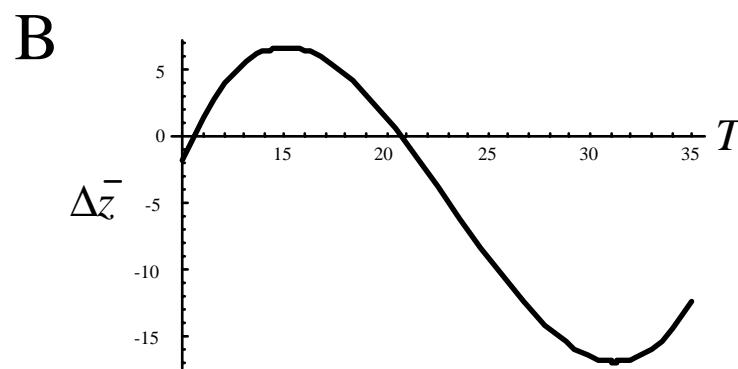
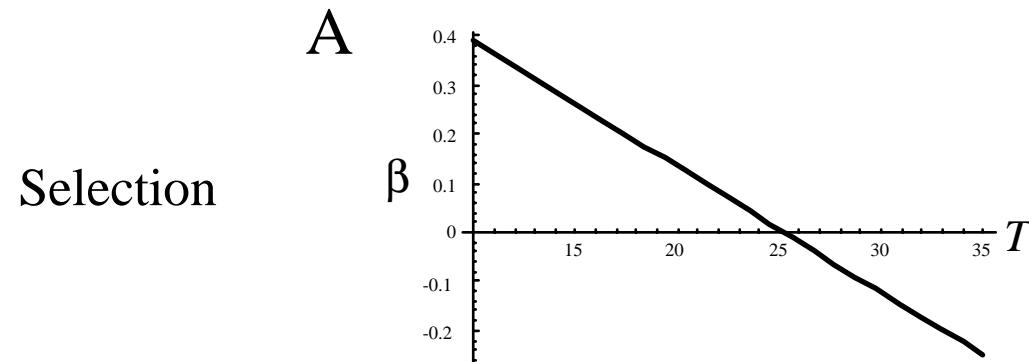


# Predicting evolutionary responses

- Mean phenotype,  $\bar{z}(T)$
- Genetic var-cov function,  $G(T, \theta))$
- Selection gradient function,  $\beta(T)$

$$\Delta\bar{z}(t) = \int G(t, s) \beta(s) ds$$

# Evolutionary Response to Selection



# Challenges

- Estimating zero eigenfunctions
- Estimation methods for  $\beta$
- Incorporating environmental information  
(distribution of T)
- Predicting evolutionary responses